

Correlation

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Correlation

- ❖ Statistical technique for measuring the relationship between variables
- ❖ If the quantities (X, Y) vary in such a way that change in one variable corresponds to change in the other variable then the variables X and Y are correlated

Methods of Studying Correlation

- ❖ Scatter diagram method
- ❖ Karl Pearson's Correlation Coefficient
- ❖ Spearman's Rank Correlation Coefficient

Scatter Plot

- ❖ Graph that is used to plot the data points for two variables
- ❖ X axis -- Independent variables
- ❖ Y axis -- Dependent Variables
- ❖ Idea about the kind of relationship between the two variables

Types of Correlation

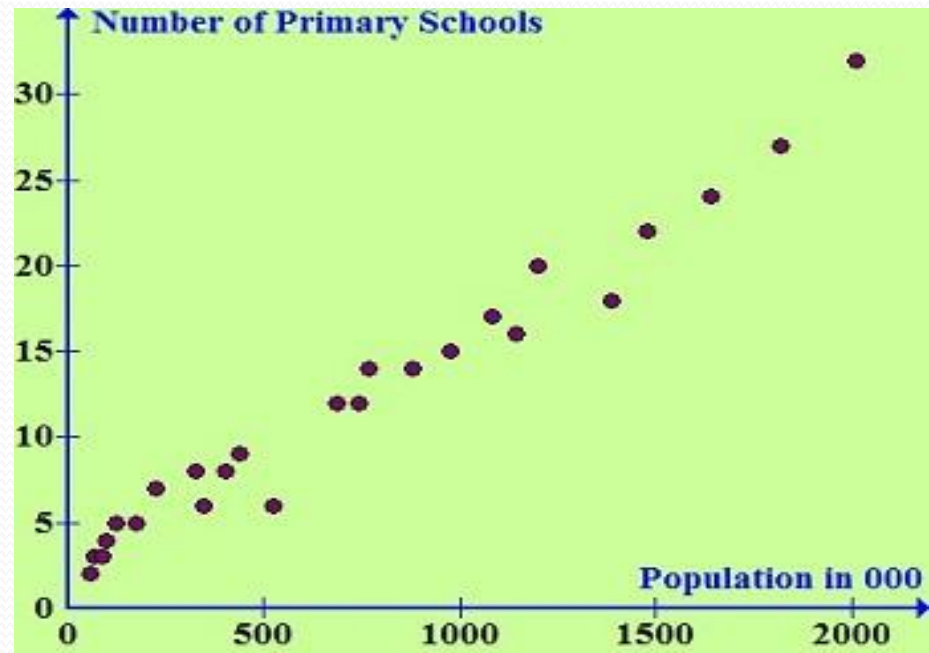
- ❖ **Positive Correlation**
- ❖ **Negative Correlation**
- ❖ **Strong Correlation**
- ❖ **Weak correlation**
- ❖ **Zero correlation**

Positive correlation

❖ X ↑, Y ↑ (increase) or X ↓, Y ↓ (decrease)

Examples

- ❖ Family income and family expenditure
- ❖ The more time you spend running on a treadmill, the more calories you will burn
- ❖ Smoking and lung diseases
- ❖ Rainfall and yield of rice
- ❖ Training and performance



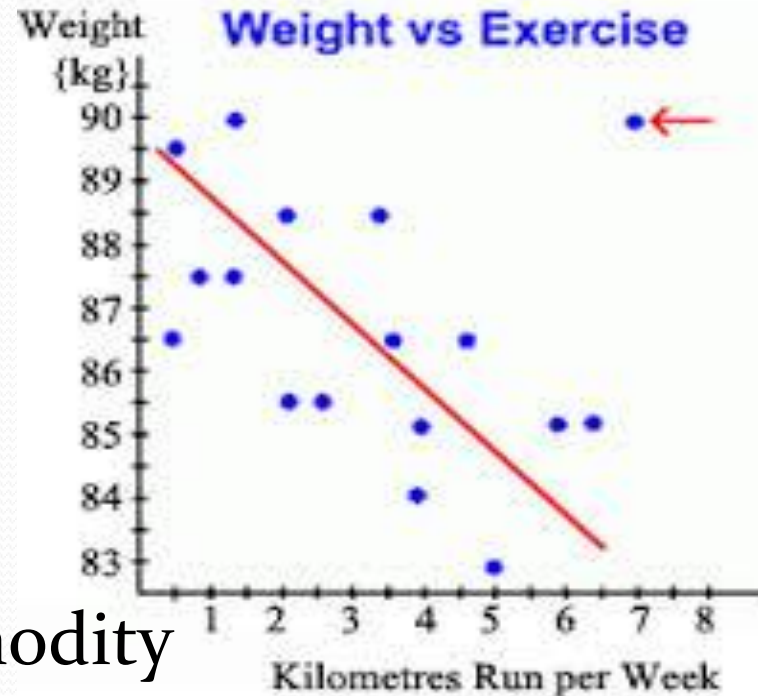
Negative correlation

❖ As X ↑, Y ↓

❖ As X ↓, Y ↑

Examples

- ❖ Demand and Price of a commodity
- ❖ Length of candle and no of hours burned
- ❖ Vaccination and illness
- ❖ School achievement and days absent from school



Zero Correlation

❖ When one factor increases/decreases we have no idea what other would be

Examples

Height of a person and income received

Correlation Coefficient

- ❖ defined as a numerical representation of the **strength** and direction of a relationship.
- ❖ Represented by “r” and unitfree
- ❖ $-1 \leq r \leq +1$
- ❖ The closer to 0, the weaker linear relationship
- ❖ No relationship if exactly equal to 0
- ❖ The closer to -1 , the stronger the negative linear relationship
- ❖ The closer to 1 , the stronger the positive linear relationship
- ❖ Exactly equal to $+1$ or -1 is perfect relationship

Three Sets of Data Showing Different Directions and Degrees of Correlation

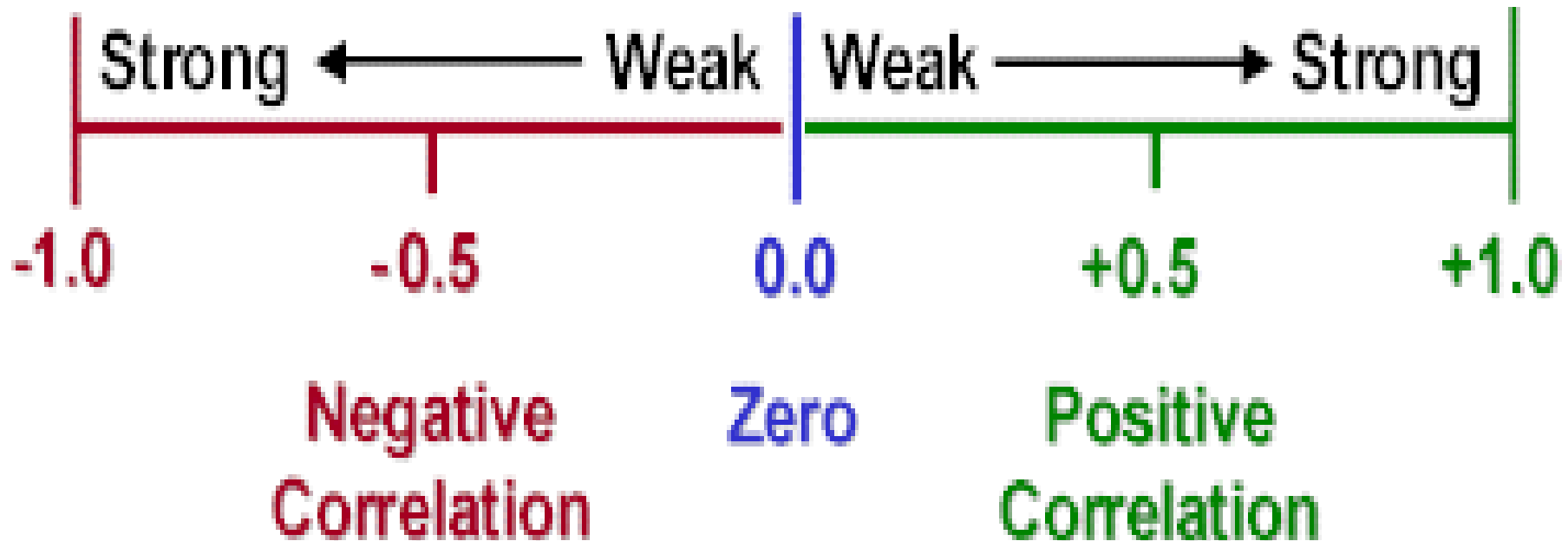
(A) $r = +1.00$		(B) $r = -1.00$		(C) $r = 0$	
X	Y	X	Y	X	Y
5	5	5	1	2	1
4	4	4	2	5	4
3	3	3	3	3	3
2	2	2	4	1	5
1	1	1	5	4	2

Interpreting Corr. Coefficient, r

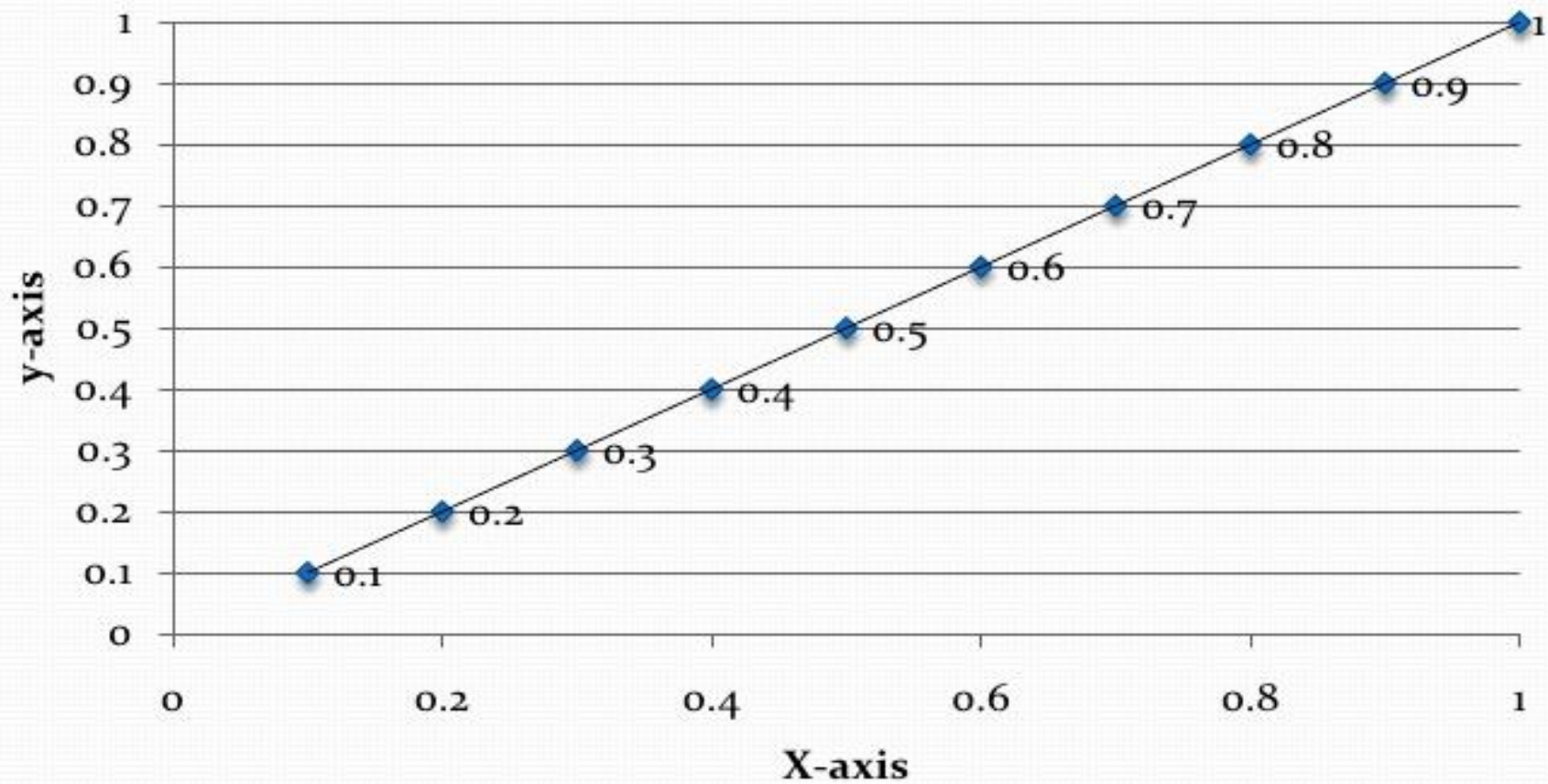
Value of Corr. Coefficient	Strength of Corr.
r equals +or- 1	Perfect
$r > .70$ or $r < -.70$	Strong
r is between $.30$ & $.70$ or r is between $-.30$ and $-.70$	Moderate
r is between 0 and $.30$ or r is between 0 and $-.30$	Weak
Equal to 0	No correlation

Correlation Coefficient

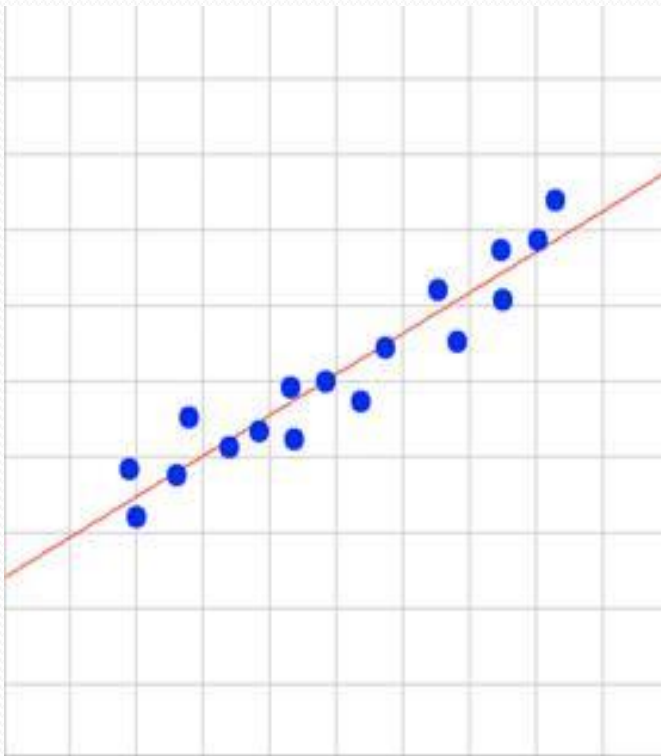
Shows Strength & Direction of Correlation



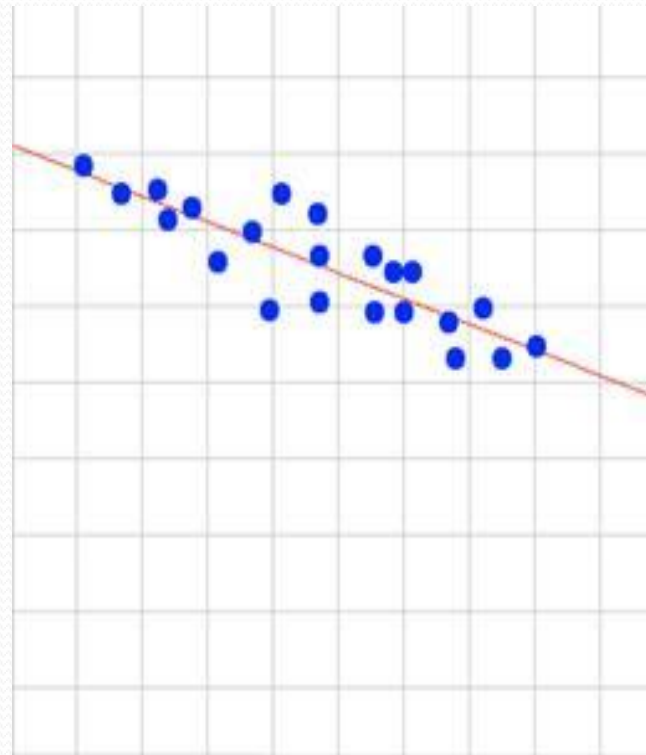
Perfect Correlation



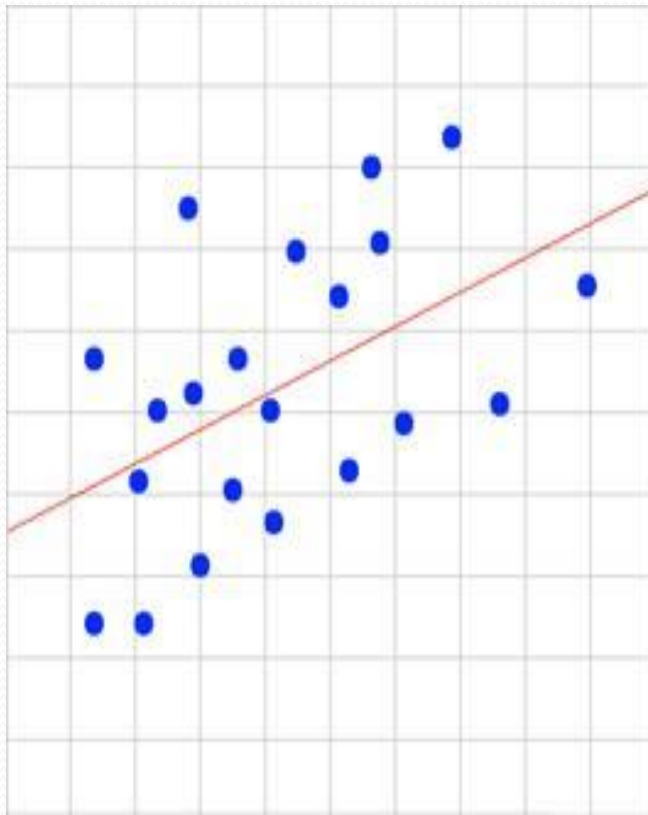
**Strong positive
correlation
 $r=0.95$**



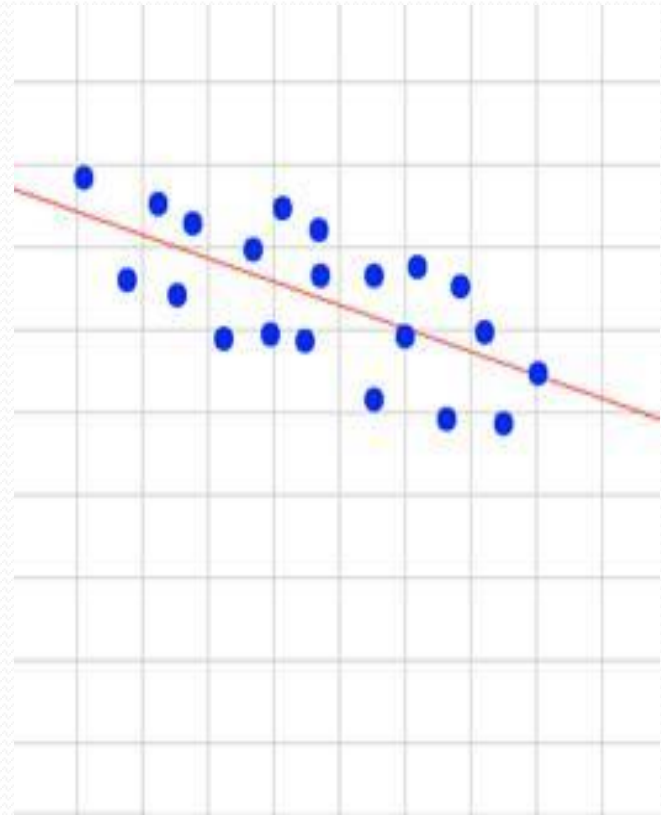
**Strong negative
correlation
 $r=-0.85$**



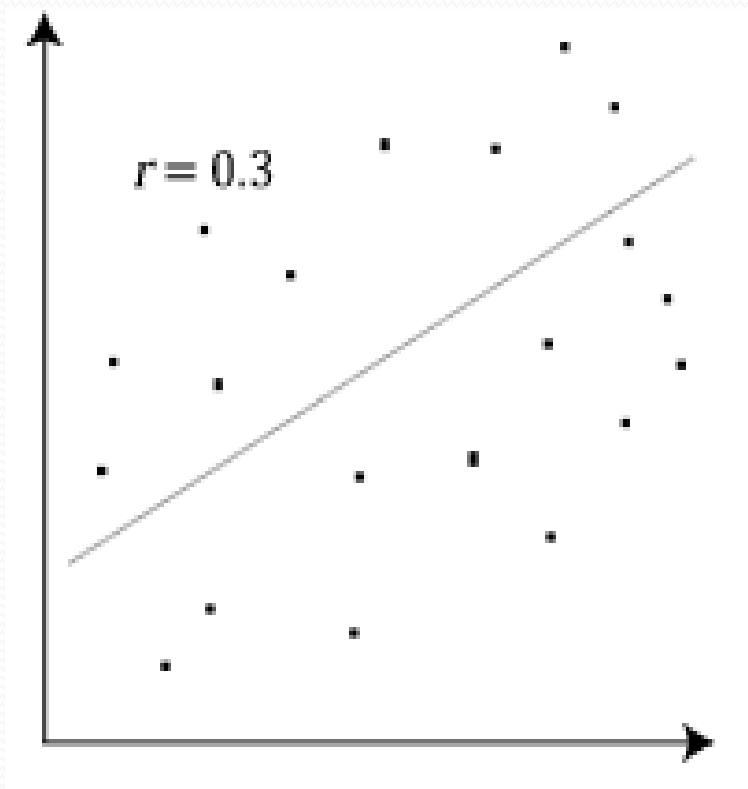
**moderate positive
correlation
 $r=0.5$**



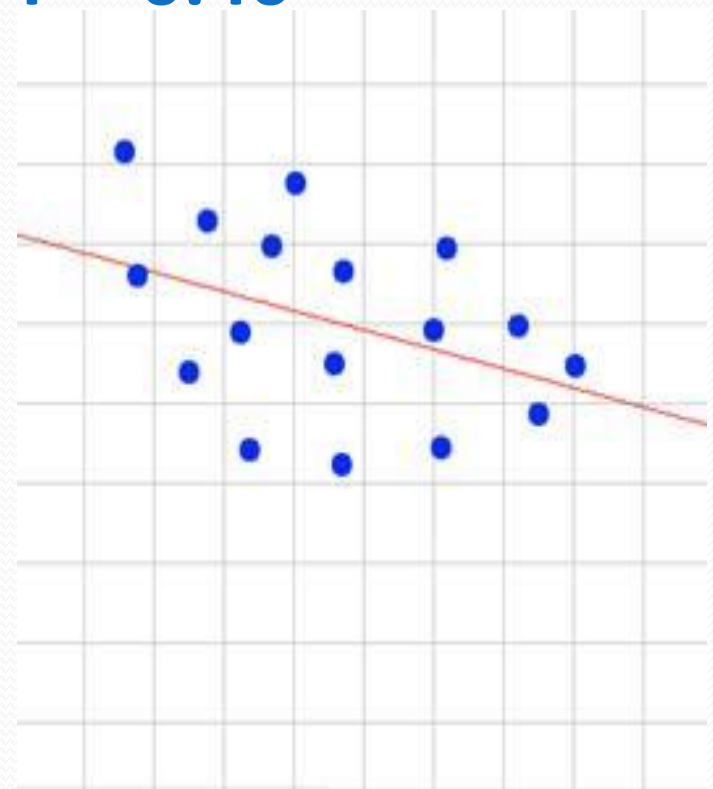
**moderate negative
correlation
 $r=-0.75$**



Weak Positive Correlation, $r=0.3$



Weak negative correlation $r = -0.40$



Pearson's Correlation coefficient

- An agricultural research organisation tested a particular chemical fertiliser to try to find out whether an increase in the fertiliser used would lead to corresponding increase in food supply

$$r_{xy} = \frac{n \sum XY - \sum X \sum Y}{\sqrt{n \sum X^2 - (\sum X)^2} \sqrt{n \sum Y^2 - (\sum Y)^2}}$$

n- sample size

X- value of Independent variable

Y-value of dependent variable

Illustration

Sl.Nos	Fertiliser (X)	Bushels of Beans(Y)	XY	X ²	Y ²
1	2	4	8	4	16
2	1	3	3	1	9
3	3	4	12	9	16
4	2	3	6	4	9
5	4	6	24	16	36
6	5	5	25	25	25
7	3	5	15	9	25

 Σ $\Sigma X =$

20

 $\Sigma Y =$

30

 $\Sigma XY =$

93

 ΣX^2

=68

 ΣY^2

=136

 $r = 0.81$

Spearman's rank coefficient

- When the values of the two variables are converted to their **ranks**, and there from the correlation is obtained, the correlations known as rank correlation
- Example: Intelligence and Beauty

$$r = 1 - \left(\frac{6 \sum d^2}{n(n^2 - 1)} \right)$$

n=No of observations

D=difference between the ranks

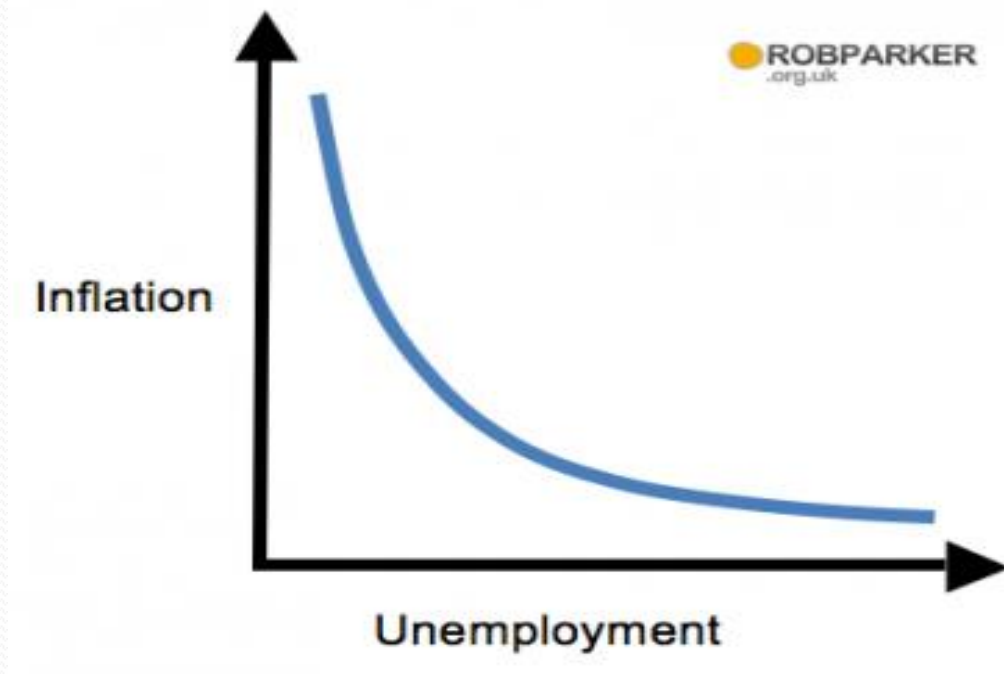
Spurious Correlation

- A situation in which measures of two or more variables are statistically related (they covary) but are not in fact causally linked—usually because the statistical relation is caused by a third variable.

Spurious Correlation

- correlation is not present in the original observations but is produced by the way the data are handled
- Example-
 1. Correlation between Long Hair and test score

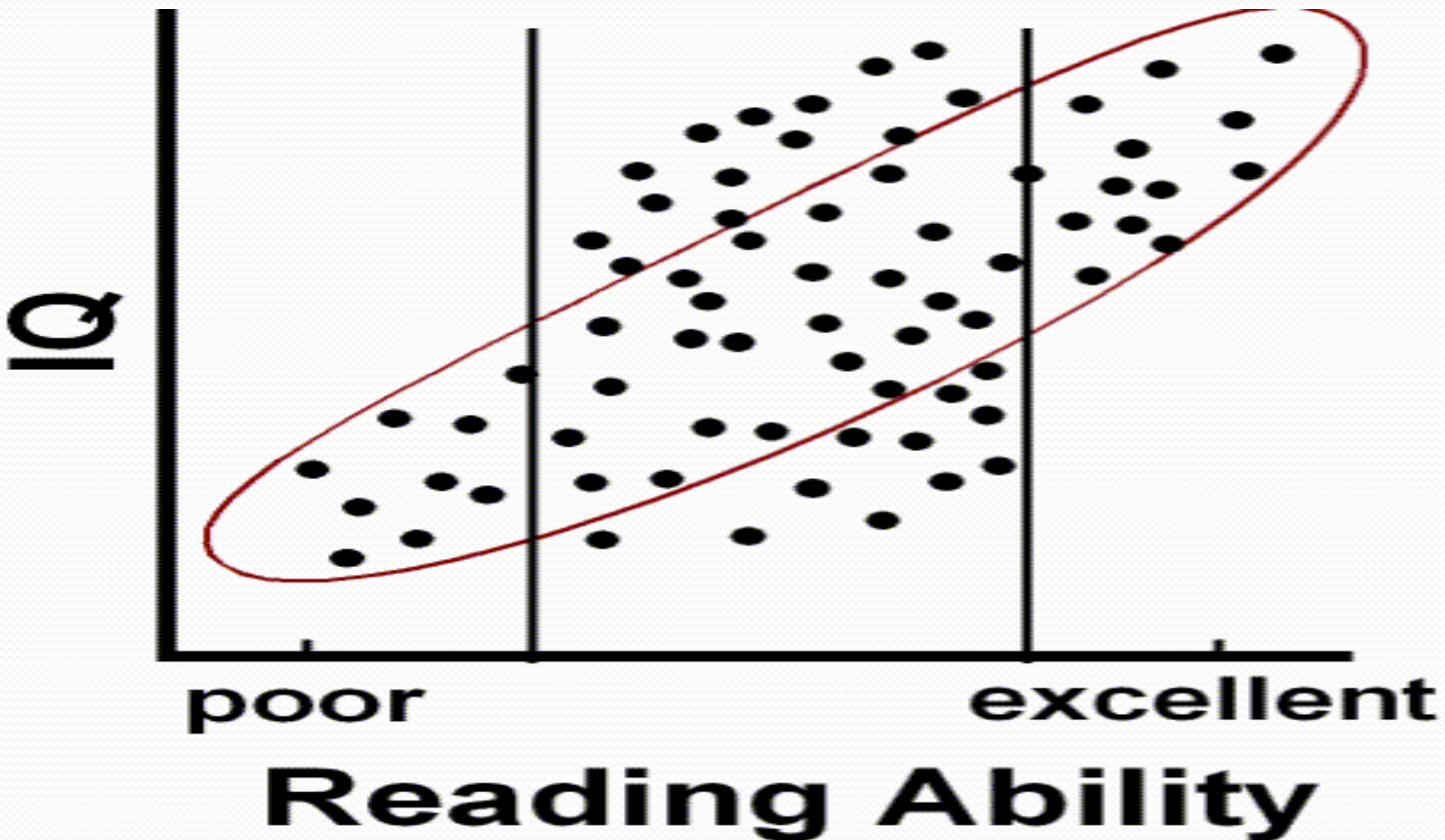
2. From economics is the Phillips curve



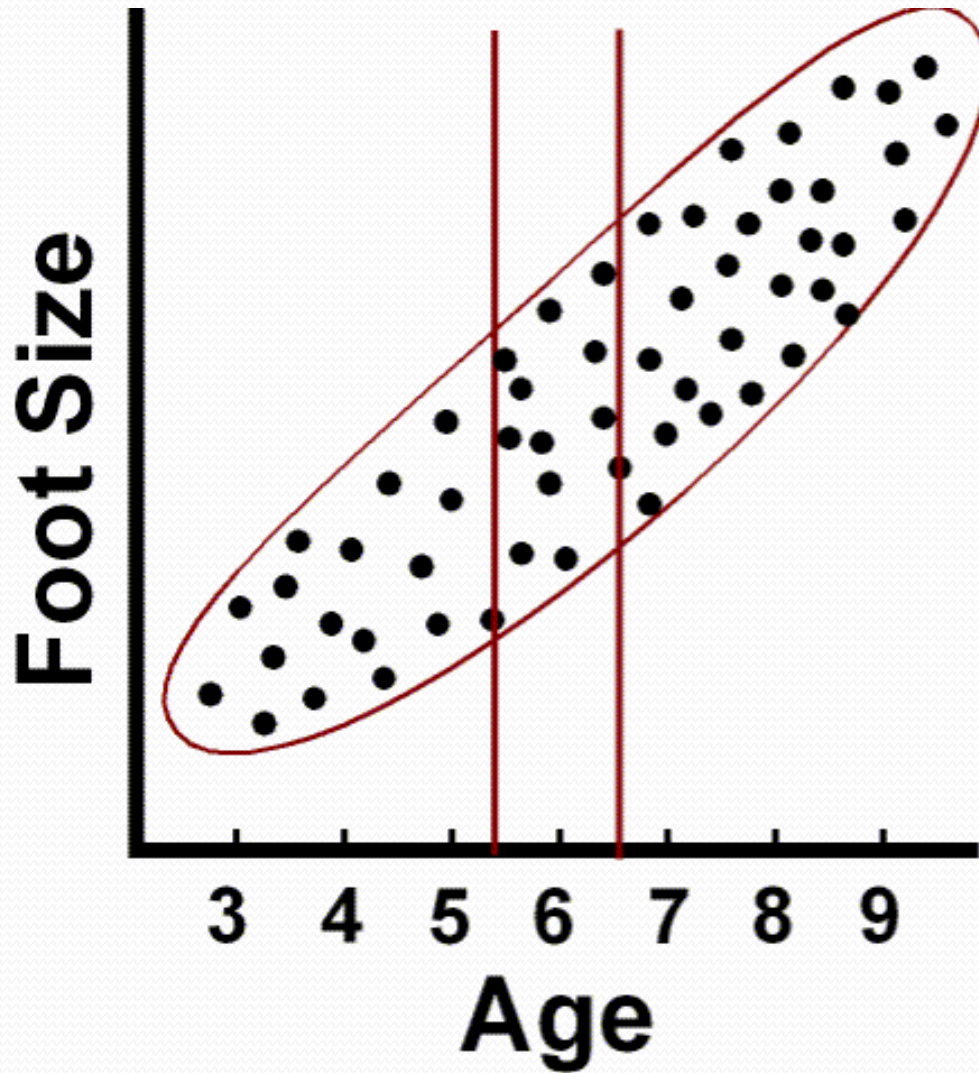
But US entered a period of Stagflation (high unemployment *and* high inflation) caused by shocks to the oil supply and government wage/price controls. (1970's)

Factors Affecting r Correlation

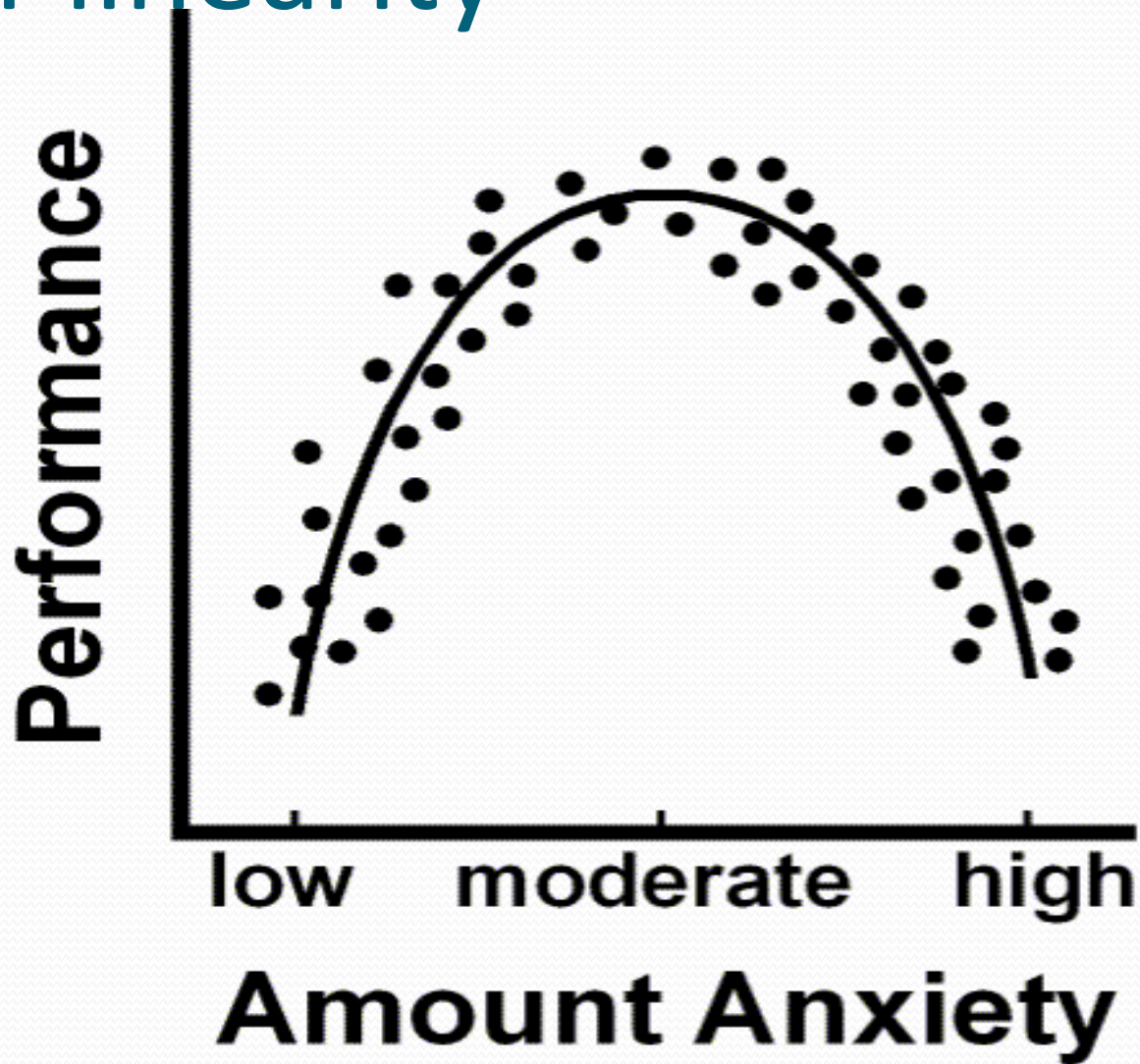
- Heterogeneous subsamples



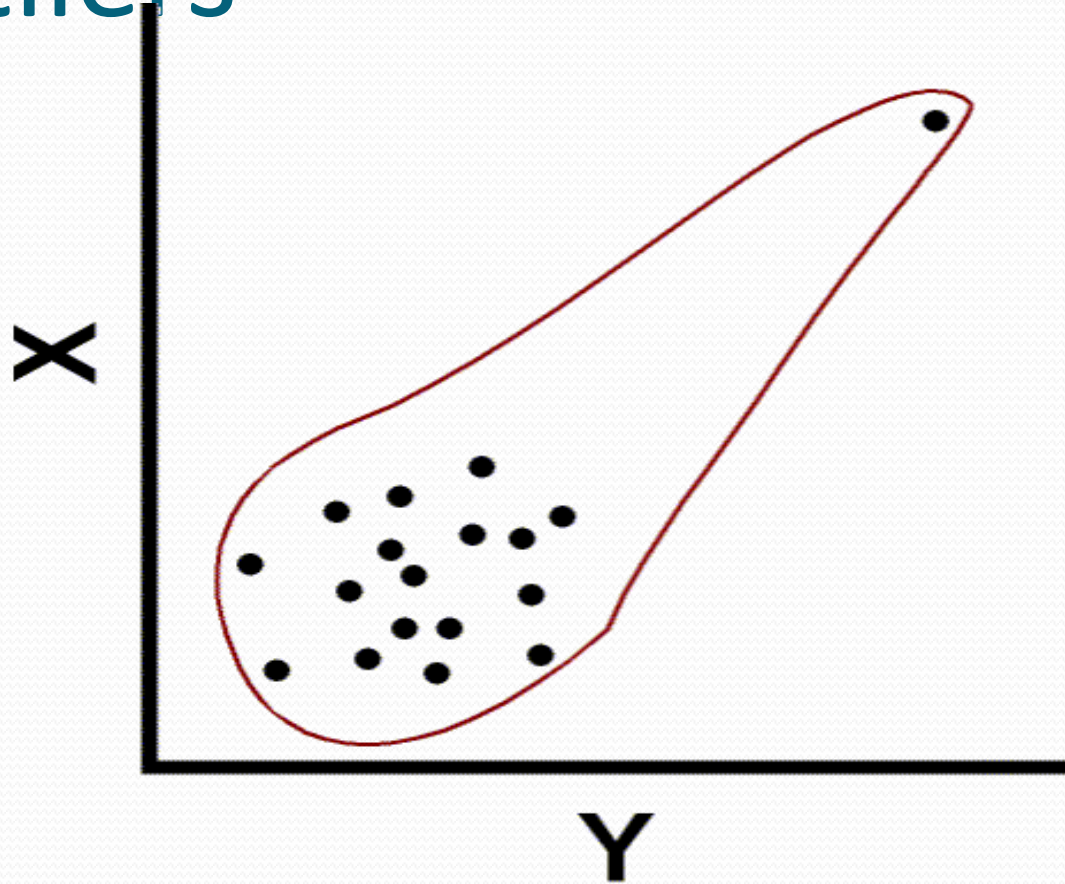
Truncation



Non-linearity



Outliers



❖ May be due to wrong measurement

An Example

Heart Disease and Smoking

- Does smoking cigarettes increase systolic blood pressure(Heart disease)?
- Data on heart disease and cigarette smoking in 21 developed countries (Landwehr and Watkins, 1987)
- Data have been rounded for computational convenience.
 - The results were not affected.

The Data

Surprisingly, the U.S. is the first country on the list--the country with the highest consumption and highest mortality.

Country	Cigarettes	CHD
1	11	26
2	9	21
3	9	24
4	9	21
5	8	19
6	8	13
7	8	19
8	6	11
9	6	23
10	5	15
11	5	13
12	5	4
13	5	18
14	5	12
15	5	3
16	4	11
17	4	15
18	4	6
19	3	13
20	3	4
21	3	14

What Does the Scatterplot Show?

- As smoking increases, so does coronary heart disease mortality.
- Fairly moderate relationship and positive
- Not all data points on line.
 - This gives us “residuals” or “errors of prediction”

Thank You...